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AUG 07 2007  
PATENT & TRADEMARK OFFICE*
1. (Currently Amended) A method of generating a pseudo-random number, said method comprising the steps of:
    - a. Establish initialization values for output series of pseudo-random number matrices  $X_1 - X_k$ ;
    - b. Store said initialized pseudo-random number matrices  $X_1 - X_k$  in number matrices storage register;
    - c. Establish initialization values for variable transition matrices  $A_{1,1} - A_{k,1}$ ;
    - d. Store said initialized transition matrices  $A_{1,1} - A_{k,1}$  in transition matrices storage register;
    - e. Establish initialization values for variable augmentation matrices  $B_{1,1} - B_{j,1}$ ;
    - f. Store said initialized augmentation matrices  $B_{1,1} - B_{j,1}$  in augmentation matrices storage register;
    - g. Establish first modulus operators  $m_{1,1} - m_{i,1}$ ;
    - h. Retrieve said transition matrices  $A_{1,1} - A_{k,1}$  and apply to said output series of pseudo-random number matrices  $X_1 - X_k$  to generate a first intermediate matrix value  $X_{\text{firsttemp}}$ ;
    - i. Retrieve said augmentation matrices  $B_{1,1} - B_{j,1}$  and apply to said first intermediate matrix value  $X_{\text{firsttemp}}$  to generate a second intermediate matrix value  $X_{\text{temp}}$ ;
    - j. Sequentially apply said first modulus operators  $m_{1,1} - m_{i,1}$  to said second intermediate matrix value  $X_{\text{temp}}$  to generate an output value of pseudo-random number matrix  $X_n$ ;
    - k. Store said first output value matrix  $X_n$  in number matrices storage register;
    - l. Retrieve and extract at least one pseudo-random number from element entries of said number matrices storage register; and
    - m. Provide said pseudo-random number to long-term storage register for use in device which can employ pseudo-random numbers.
  2. (Currently Amended) A method of generating a plurality of pseudo-random numbers, said method comprising the steps of:
    - a. Establish initialization values for output series of pseudo-random number matrices  $X_1 - X_k$ ;
    - b. Store said initialized pseudo-random number matrices  $X_1 - X_k$  in number matrices storage register;
    - c. Establish initialization values for variable transition matrices  $A_{1,1} - A_{k,1}$ ;
    - d. Store said initialized transition matrices  $A_{1,1} - A_{k,1}$  in transition matrices storage register;
    - e. Establish initialization values for variable augmentation matrices  $B_{1,1} - B_{j,1}$ ;
    - f. Store said initialized augmentation matrices  $B_{1,1} - B_{j,1}$  in augmentation matrices storage register;
    - g. Establish first modulus operators  $m_{1,1} - m_{i,1}$ ;
    - h. Retrieve said transition matrices  $A_{1,1} - A_{k,1}$  and apply to said output series of pseudo-random number matrices  $X_1 - X_k$  to generate a first intermediate matrix value  $X_{\text{firsttemp}}$ ;
    - i. Retrieve said augmentation matrices  $B_{1,1} - B_{j,1}$  and apply to said first intermediate matrix value  $X_{\text{firsttemp}}$  to generate a second intermediate matrix value  $X_{\text{temp}}$ ;
    - j. Sequentially apply said first modulus operators  $m_{1,1} - m_{i,1}$  to said second intermediate matrix value  $X_{\text{temp}}$  to generate a first output value of pseudo-random number matrix  $X_n$ ;
    - k. Store said first output value matrix  $X_n$  in said number matrices storage register to establish an updated output series of pseudo-random number matrices  $X_{n-k+1} - X_n$ ;
    - l. Retrieve and extract at least one pseudo-random number from element entries of said number matrices storage register;
    - m. Provide each pseudo-random number to long-term storage register for use in device which can employ pseudo-random numbers;
    - n. Retrieve and update said transition matrices  $A_{1,1} - A_{k,1}$  through updating process to create and store updated transition matrices  $A_{1,2} - A_{k,2}$ ;

- o. Retrieve said updated transition matrices  $A_{1,2} - A_{k,2}$  and apply to said updated output series of pseudo-random number matrices  $X_{n-k+1} - X_n$  to generate an updated first intermediate matrix value  $X_{firsttemp}$ ;
  - p. Retrieve and update said augmentation matrices  $B_{1,1} - B_{j,1}$  through updating process to create and store updated augmentation matrices  $B_{1,2} - B_{j,2}$ ;
  - q. Retrieve said updated augmentation matrices  $B_{1,2} - B_{j,2}$  and apply to said updated first intermediate matrix value  $X_{firsttemp}$  to generate an updated second intermediate matrix value  $X_{temp}$ ;
  - r. Update said first modulus operators  $m_{1,1} - m_{i,1}$  through updating process to create updated first modulus operators  $m_{1,2} - m_{i,2}$ ;
  - s. Sequentially apply said updated first modulus operators  $m_{1,2} - m_{i,2}$  to said updated second intermediate matrix value  $X_{temp}$  to generate a second output value of pseudo-random number matrix  $X_{n+1}$  from which at least one pseudo-random number is extracted; and
  - t. Store said second pseudo-random number matrix  $X_{n+1}$  in said number matrices storage register.
3. (Currently Amended) A method of generating a plurality of pseudo-random numbers according to claim 2, wherein said steps l. through t. are repeated to generate a desired number d of pseudo-random number matrices  $X_{n+d}$  from which a plurality of element entries of said pseudo-random number matrices are extracted as pseudo-random numbers and provided to long-term storage register for use in device which can employ pseudo-random numbers.
4. (Original) A method according to claim 2 further comprising the step of:  
Selecting a first subset of said pseudo-random numbers from said updated output series of pseudo-random number matrices.
5. (Original) A method according to claim 1, claim 2, or claim 3, wherein  $k = 1$  so that a single variable transition matrix is used.
6. (Currently Amended) A method according to claim 1, claim 2, or claim 3, where  $j = 1$  so that a single variable augmentation matrix is used.
7. (Original) A method according to claim 1, claim 2, or claim 3, where  $i = 1$  so that a single modulus operator is used.
8. (Original) A method according to claim 2, further comprising the steps of:
  - a. Establish second modulus operators  $r_{1,1} - r_{g,1}$ ;
  - b. Sequentially apply and update second modulus operators  $r_{1,1} - r_{g,1}, r_{1,2} - r_{g,2}, \dots r_{1,n+d-k} - r_{g,n+d-k}$  to said updated output series of pseudo-random number matrices to generate a second output series of pseudo-random number matrices.
9. (Currently Amended) A method according to claim 8, further comprising the step of:  
Selecting a second subset of said pseudo-random numbers from element entries of said second output series of pseudo-random number matrices.
10. (Original) A method according to claim 1, claim 2, or claim 3:
  - a. Wherein said first modulus operators  $m_{1,1} - m_{j,1}, m_{1,2} - m_{j,2}, \dots m_{1,n+d-k} - m_{j,n+d-k}$  comprise a uniform variable modular reduction, and
  - b. Further comprising the step of discarding certain pseudo-random numbers which are not uniformly distributed.
11. (Original) A method according to claim 8:

- a. Wherein said second modulus operators  $r_{1,1} - r_{g,1}, r_{1,2} - r_{g,2}, \dots r_{1,n+d-k} - r_{g,n+d-k}$  comprise a uniform variable modular reduction, and
  - b. Further comprising the step of discarding certain pseudo-random numbers which are not uniformly distributed.
12. (Currently Amended) A method according to claim 2 or claim 3, further comprising the steps of:
- a. Create at least one alternate storage register of pseudo-random number matrices by separately taking steps a – t;
  - b. Create temporary composite pseudo-random number matrices by combining each resulting storage register of pseudo-random number matrices through at least one mathematical operation;
  - c. Create final composite pseudo-random number matrices by applying variable modular reduction to said temporary composite pseudo-random number matrices; and
  - d. Select a subset of pseudo-random numbers from element entries of said resulting final composite pseudo-random number matrices.
13. (Currently Amended) A method according to claim 1, claim 2, or claim 3 further comprising:
- a. Apply an invertibility evaluation module to each second intermediate matrix value  $X_{temp}$ ;
  - b. Adjust augmentation matrices  $B_{1,1} - B_{j,1}, B_{1,2} - B_{j,2}, \dots B_{1,n+d-1} - B_{j,n+d-1}$ , so that said second intermediate matrix value  $X_{temp}$  is non-invertible;
  - c. Sequentially apply said first modulus operators  $m_{1,1} - m_{i,1}$  to said non-invertible second intermediate matrix value  $X_{temp}$  to generate output value of non-invertible pseudo-random number matrix  $X_n$  from which at least one pseudo-random number is extracted; and
  - d. Select a subset of pseudo-random number output values from element entries of said non-invertible pseudo-random number matrices.
14. (Currently Amended) An apparatus for generating a pseudo-random number, said apparatus comprising:
- a. Output matrices initialization means for establishing and storing initialization values for output series of pseudo-random number matrices  $X_1 - X_k$  by assigning values to matrix entries;
  - b. Transition matrices initialization means for establishing and storing initialization values for variable transition matrices  $A_{1,1} - A_{k,1}$  by assigning values to matrix entries;
  - c. Augmentation matrices initialization means for establishing and storing initialization values for variable augmentation matrices  $B_{1,1} - B_{j,1}$  by assigning values to matrix entries;
  - d. Modulus operator initialization means for establishing first modulus operators  $m_{1,1} - m_{i,1}$  by assigning values to modulus operators;
  - e. First application means for retrieving and applying said transition matrices  $A_{1,1} - A_{k,1}$  to said output series of pseudo-random number matrices  $X_1 - X_k$  to generate a first intermediate matrix value  $X_{firsttemp}$ ;
  - f. Second application means for retrieving and applying said augmentation matrices  $B_{1,1} - B_{j,1}$  to said first intermediate matrix value  $X_{firsttemp}$  to generate a second intermediate matrix value  $X_{temp}$ ; and
  - g. Third application means for sequentially applying said first modulus operators  $m_{1,1} - m_{i,1}$  to said second intermediate matrix value  $X_{temp}$  to generate and store an output value of pseudo-random number matrix  $X_n$  from element entries of which at least one pseudo-random number is extracted and provided to long-term storage for use in device which can employ pseudo-random numbers.

15. (Currently Amended) An apparatus for generating a plurality of pseudo-random numbers, said apparatus comprising:
- a. Output matrices initialization means for establishing and storing initialization values for output series of pseudo-random number matrices  $X_1 - X_k$  by assigning values to matrix entries;
  - b. Transition matrices initialization means for establishing and storing initialization values for variable transition matrices  $A_{1,1} - A_{k,1}$  by assigning values to matrix entries;
  - c. Augmentation matrices initialization means for establishing and storing initialization values for variable augmentation matrices  $B_{1,1} - B_{j,1}$  by assigning values to matrix entries;
  - d. Modulus operator initialization means for establishing first modulus operators  $m_{1,1} - m_{i,1}$  by assigning values to modulus operators;
  - e. First application means for retrieving and applying said transition matrices  $A_{1,1} - A_{k,1}$  to said output series of pseudo-random number matrices  $X_1 - X_k$  to generate a first intermediate matrix value  $X_{\text{firsttemp}}$ ;
  - f. Second application means for retrieving and applying said augmentation matrices  $B_{1,1} - B_{j,1}$  to said first intermediate matrix value  $X_{\text{firsttemp}}$  to generate a second intermediate matrix value  $X_{\text{temp}}$ ;
  - g. Third application means for sequentially applying said first modulus operators  $m_{1,1} - m_{i,1}$  to said second intermediate matrix value  $X_{\text{temp}}$  to generate and store a first output value of pseudo-random number matrix  $X_n$  from element entries of which at least one pseudo-random number is extracted and provided to long-term storage for use in device which can employ pseudo-random numbers;
  - h. Storage means for storing said first output value matrix  $X_n$  in a storage register to establish an updated output series of pseudo-random number matrices;
  - i. Transition matrices updating means for retrieving and updating said transition matrices  $A_{1,1} - A_{k,1}$  to create and store updated transition matrices  $A_{1,2} - A_{k,2}$ ;
  - j. Fourth application means for retrieving and applying said updated transition matrices  $A_{1,2} - A_{k,2}$  to said updated output series of pseudo-random number matrices  $X_{n-k+1} - X_n$  to generate an updated first intermediate matrix value  $X_{\text{firsttemp}}$ ;
  - k. Augmentation matrices updating means for retrieving and updating said augmentation matrices  $B_{1,1} - B_{j,1}$  to create and store updated augmentation matrices  $B_{1,2} - B_{j,2}$ ;
  - l. Fifth application means for retrieving and applying said updated augmentation matrices  $B_{1,2} - B_{j,2}$  to said updated first intermediate matrix value  $X_{\text{firsttemp}}$  to generate an updated second intermediate matrix value  $X_{\text{temp}}$ ;
  - m. Modulus operator updating means for updating said first modulus operators  $m_{1,1} - m_{i,1}$  to create updated first modulus operators  $m_{1,2} - m_{i,2}$ ;
  - n. Sixth application means for sequentially applying said updated first modulus operators  $m_{1,2} - m_{i,2}$  to said updated second intermediate matrix value  $X_{\text{temp}}$  to generate a second output value of pseudo-random number matrix  $X_{n+1}$  from element entries of which at least one pseudo-random number is extracted and provided to long-term storage register for use in device which can employ pseudo-random numbers; and
  - o. Second storage means for storing said second pseudo-random number matrix  $X_{n+1}$  in said number matrices storage register.